

Temporal convolutions

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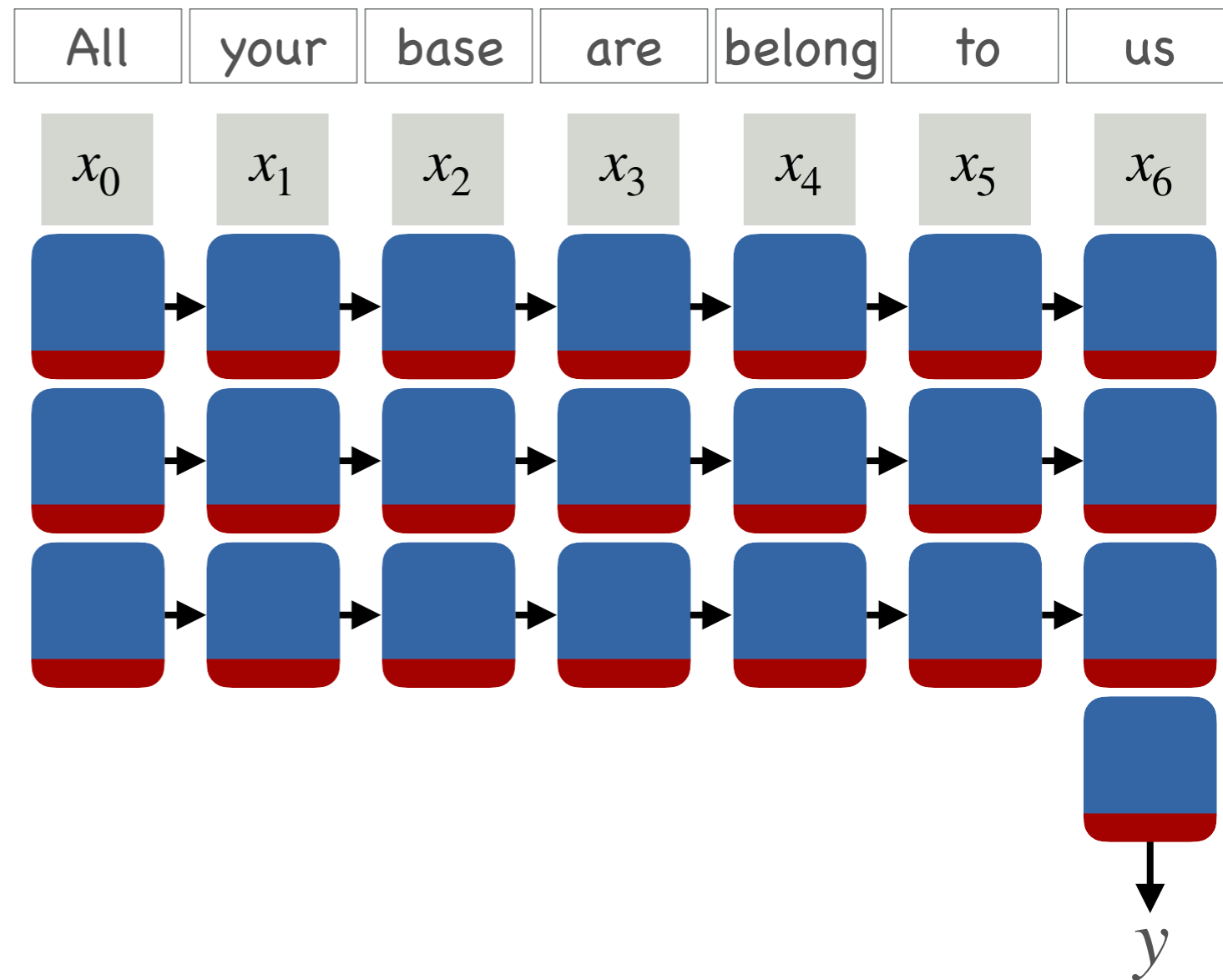
Recurrent models

- Advantages

- Variable input length
- Variable output length
- Structured output

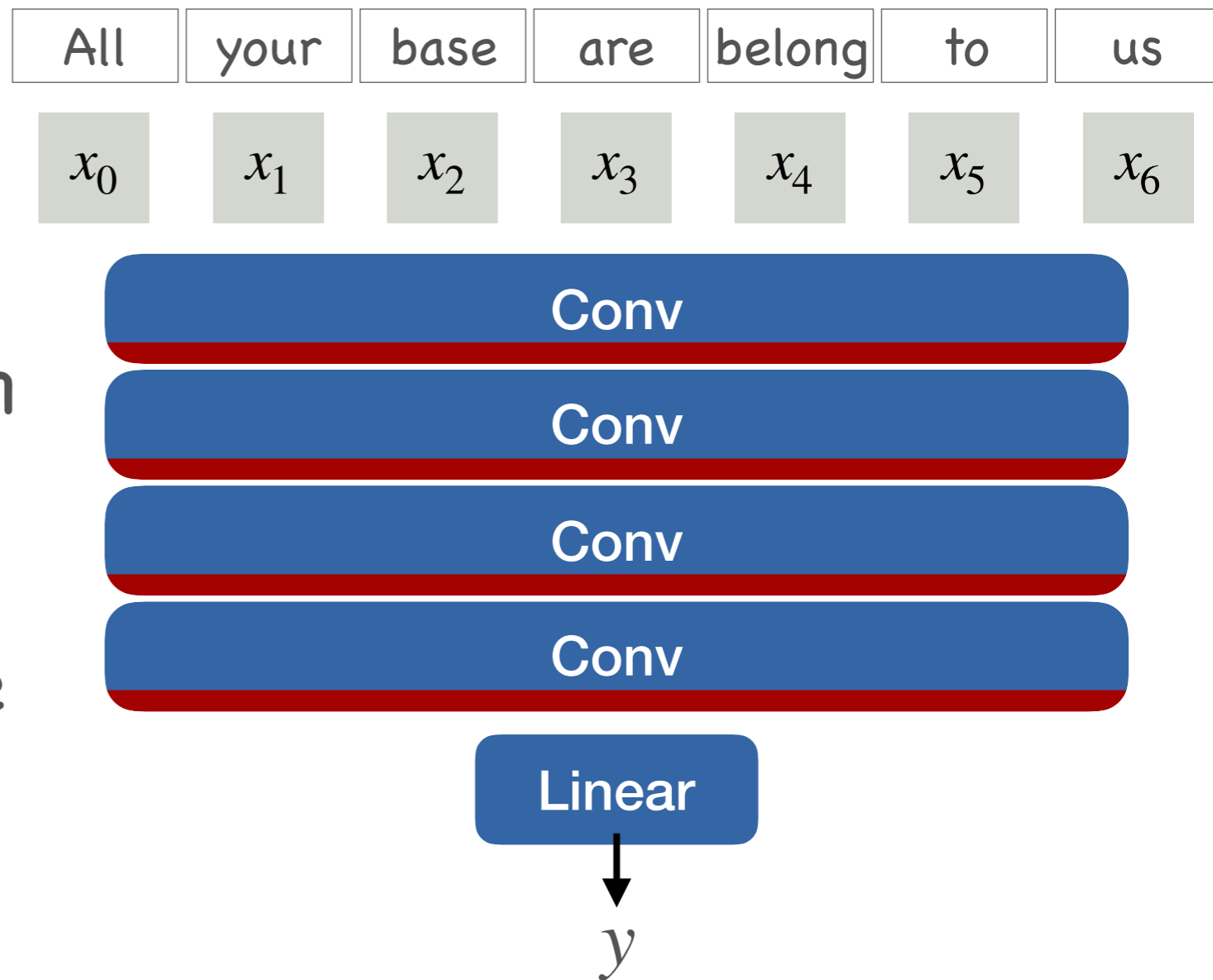
- Disadvantage

- Hard to train
- Cannot learn dependencies longer than 100 steps



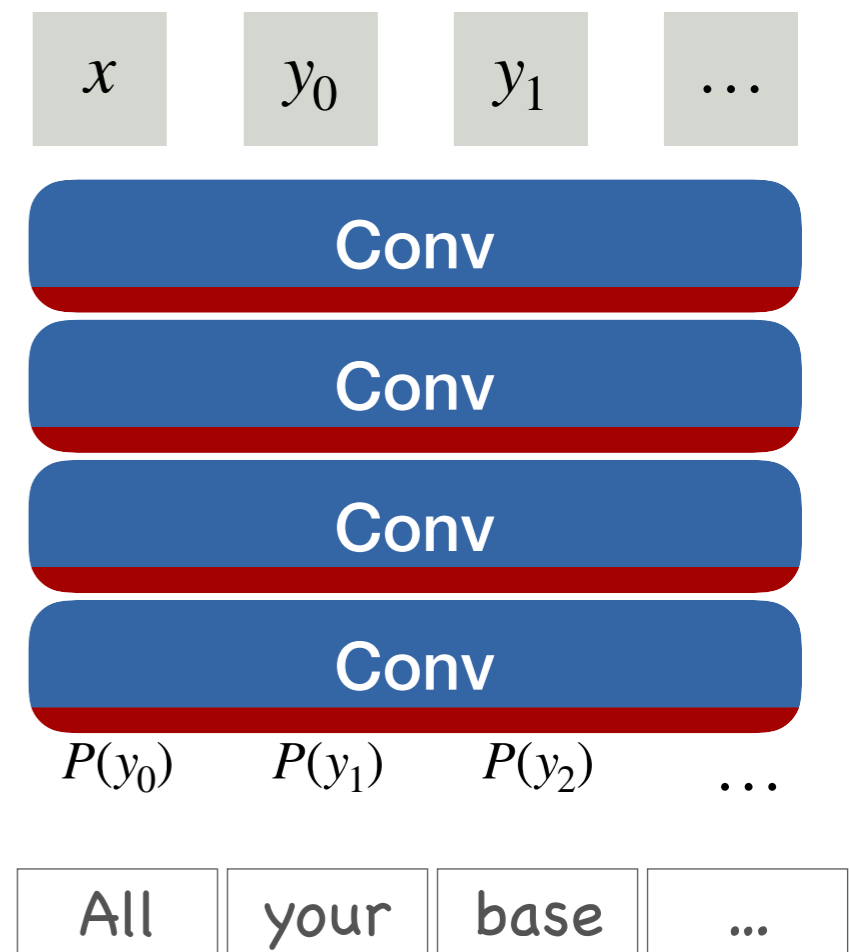
Temporal convolutional networks

- Dilated convolution
- Exponential growth in receptive field
- 5-10 layers, receptive field > 100 steps



Sequence generation using convolutions

- Causal (masked) convolutions
- Only look into past
- Auto-regressive model
 - $P(y_0 | x) \cdot P(y_1 | x, y_0) \cdot P(y_2 | x, y_0, y_1) \cdot \dots$



- Conditional image generation with pixelcnn decoders, Van den Oord et al., *NIPS* 2016
- WaveNet: A generative model for raw audio, Van Den Oord et al., *arXiv* 2016

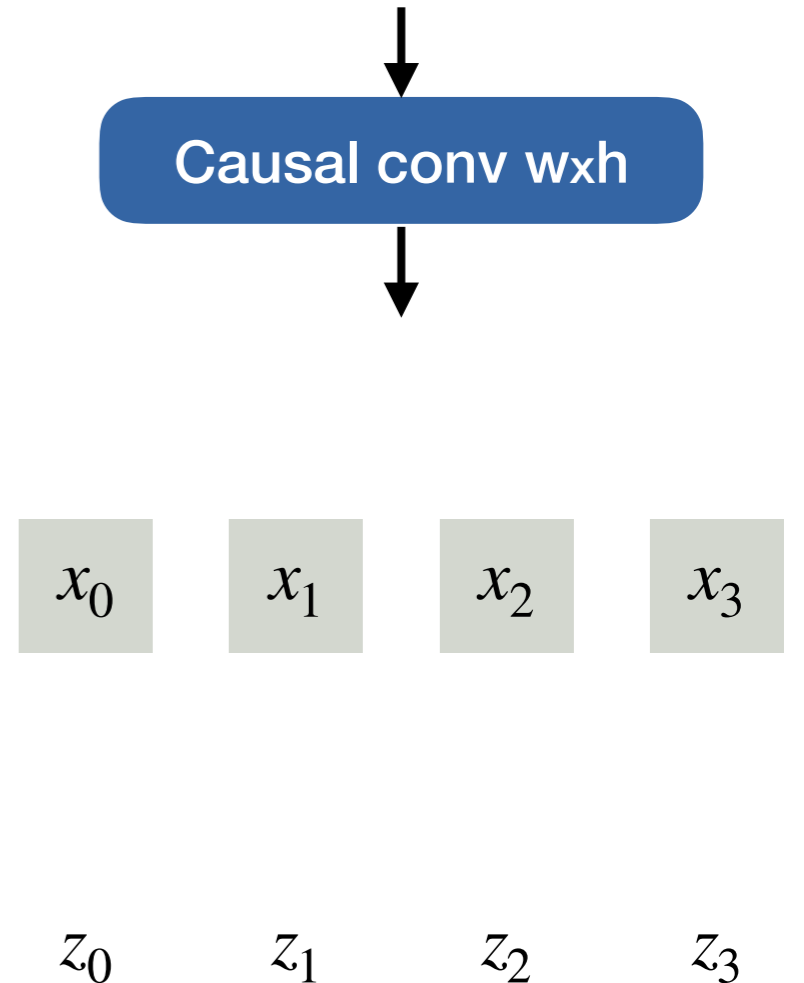
Causal convolution

- Input: $\mathbf{X} \in \mathbb{R}^{T \times C_1}$

- Kernel: $\mathbf{w} \in \mathbb{R}^{w \times C_1 \times C_2}$

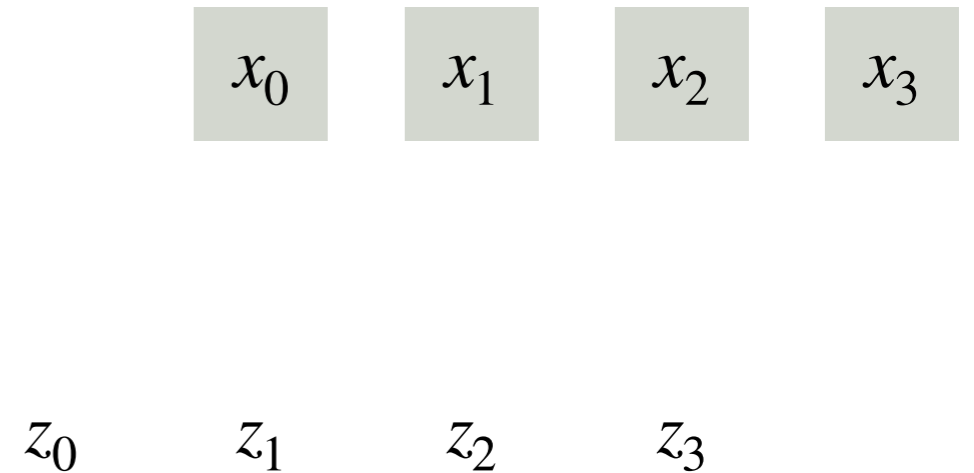
- Bias: $\mathbf{b} \in \mathbb{R}^{C_2}$

- Output:
$$\mathbf{Z}_{t,b} = \mathbf{b}_c + \sum_{i=0}^{w-1} \sum_{j=0}^{C_1-1} \mathbf{X}_{t+i-w,b+j} \mathbf{w}_{i,j}$$



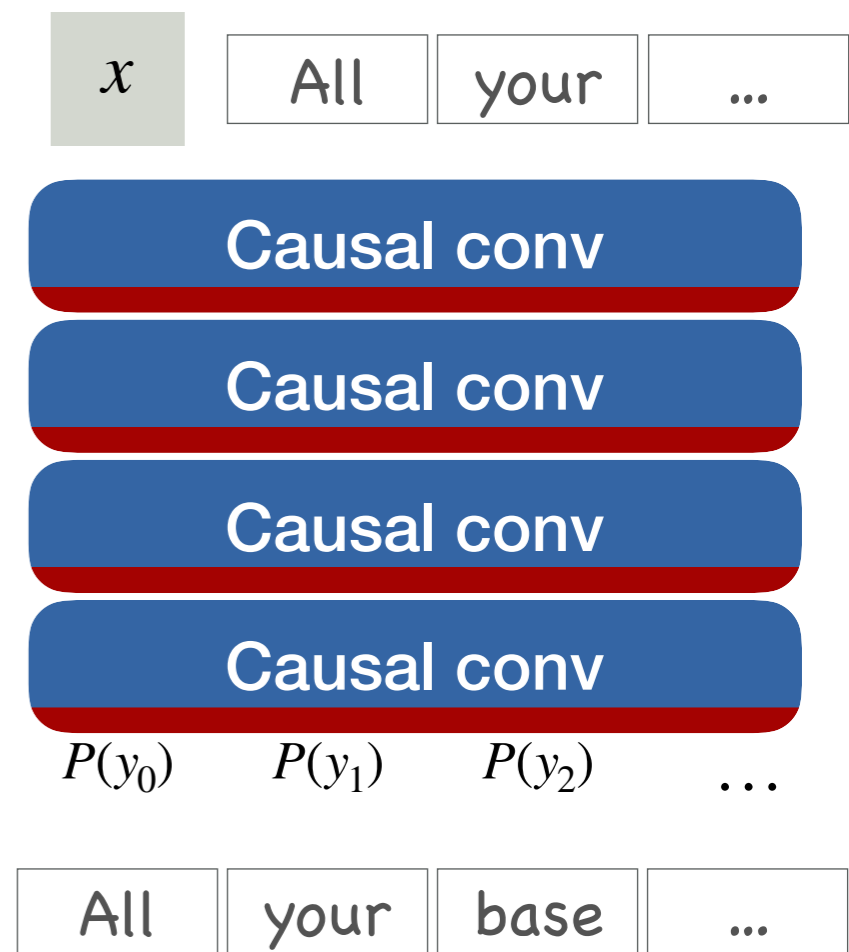
Causal convolution implementation

- Regular convolution
 - Shift output



Training with temporal convolutions

- Labels
 - input and output/loss
- Very efficient
 - fully convolutional



Inference with temporal convolutions

- Step by step
- Harder to implement efficiently

