

$$\mathbb{E}_{a \sim P_\theta} [g_\theta(a)] = \int_{\tilde{\Omega}} P(b) \, g_\theta(b\sigma_\theta + \mu_\theta) db$$